

# 以運算放大器實現模糊歸屬函數之類比電路 OPA Based Analog Circuit for Fuzzy Membership Functions

侯俊禮\* 陳世翔 洪君維

Chun-Li Hou\*, Shih-Hsiang Chen, Jiun-Wei Horng

## 摘要

本文利用兩個運算放大器和一個超級二極體來實現模糊理論中的歸屬函數電路合成。藉由運算放大器適當的偏壓製造出片段線性曲線。調整電路內部大量的電阻來獲得所需片段線性曲線的斜率。運算放大器使用一般的 UA741 而超級二極體則由運算放大器和一個二極體組成。超級二極體連接在輸出端。而商業用運算放大器有著非常廣大的用途。

關鍵詞：模糊歸屬函數，運算放大器，類比電路

## Abstract

In this paper, two OPAs and a superdiode are used to realize the circuit of a fuzzy membership function. It allows the piecewise linear curve to be generated by biasing the OPAs properly. A lot of variable resistors are adjusted to obtain the required slope of the piecewise linear curve. The OPAs adopts the common UA741 ICs and the superdiode composed of an OPA and a diode. The superdiode is connected in the output end. The commercially available operational amplifiers are widely used in practical applications.

Keywords: fuzzy membership function, operational amplifier, analog circuit

## I. INTRODUCTION

Fuzzy theory has been developed for decades in [1]. It has been extensively applied to various fields in [2-5]. For example, machinery controls, electronics, chemistry, civil engineering, automobiles, and electric machine, etc. The most important application is the fuzzy controlling. This circuit can be applied as the next stage of the detecting devices. The circuit corresponds to the tenuity signals as temperature or pressure received by sensors to the location on the fuzzy distribution curve. There are few research to realize fuzzy membership function with discrete circuit in the past [6]. So the circuit mentioned here is very important for the extensively using OPAs in industry.

## II. FUZZY MEMBERSHIP FUNCTION

The fuzzy membership function is used to show fuzzy degree in [7-8]. According to the figure, a common fuzzy membership function can be divided into three big classes: Triangular, Trapezoidal and Bell-shaped. The triangular membership function is such as Equation (1) and Fig. 1.

$$A(x) = \begin{cases} b \left( 1 - \frac{|x-a|}{s} \right) & \text{when } a-s \leq x \leq a+s \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

The trapezoidal membership function is such as Equation (2) and Fig. 2.

$$A(x) = \begin{cases} \frac{(a-x)e}{a-b} & \text{when } a \leq x \leq b \\ e & \text{when } b \leq x \leq c \\ \frac{(d-x)e}{d-c} & \text{when } c \leq x \leq d \\ 0 & \text{otherwise} \end{cases} \quad (2)$$

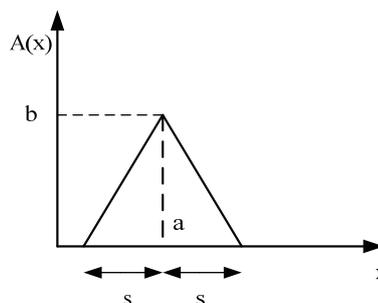


Fig. 1 The triangular membership function

The bell-shaped membership function is such as Equation (3) and Fig. 3.

$$A(x) = ce^{-\frac{(x-a)^2}{b}} \quad (3)$$

The function represents the fuzzy degree of observed object. The object is absolute match our subjective definition if the value is maximum. The minimum is opposite.

### III. CIRCUIT CONFIGURATION

#### 1. Inverting operational amplifier

Fig. 4 shows an inverting amplifier. The voltage of the noninverting terminal is obtained from  $V_{cc}$  and  $-V_{ee}$ . According to the superposition theorem and amplifier theory, if  $V_{ee}=V_{cc}$  we can get:

$$V_{o1} = -\frac{R_2}{R_1} V_i + \left(\frac{R_1 + R_2}{R_1}\right) \left(\frac{R_4 - R_3}{R_4 + R_3}\right) V_{CC} \quad (4)$$

if  $V_{o1} = 0$  we find the horizontal intercept in Figure 5:

$$V_i' = \left(\frac{R_1 + R_2}{R_2}\right) \left(\frac{R_4 - R_3}{R_4 + R_3}\right) V_{CC} \quad (5)$$

Fig. 5 shows the transfer curve of the inverting amplifier. We can adjust  $R_1$  and  $R_2$  to control the slope of the curve. And from Equation (5), the horizontal intercept is tunable by resistors  $R_3$  and  $R_4$  and  $V_{cc}$ .

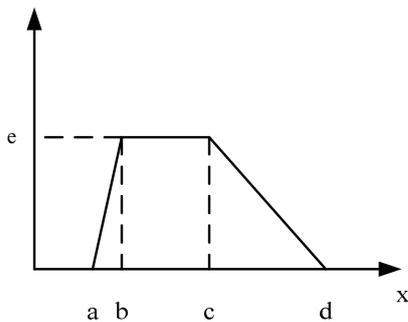


Fig. 2 The trapezoidal membership function

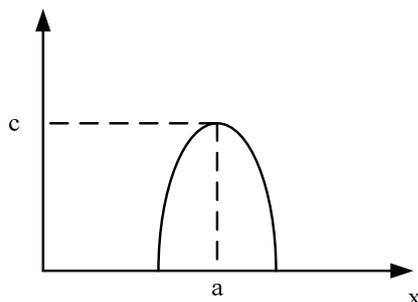


Fig. 3 The bell-shaped membership function

#### 2. Noninverting operational amplifier

Fig. 6 shows a noninverting amplifier. The voltage of the noninverting terminal of the amplifier is obtained from  $V_{cc}$  and  $-V_{ee}$ . According to the superposition theorem and the amplifier theory, if  $V_{ee}=V_{cc}$  we can find

$$V_{o2} = \left(\frac{R_8 + R_9}{R_8}\right) \left\{ \frac{R_5 R_6 V_i + [R_6 R_7 - R_5 R_7] V_{CC}}{R_5 R_6 + R_5 R_7 + R_6 R_7} \right\} \quad (6)$$

if  $V_{o2} = 0$  the horizontal intercept

$$V_i^* = \frac{R_5 R_7 - R_6 R_7}{R_5 R_6} V_{CC} \quad (7)$$

Fig. 7 shows the transfer curve of the noninverting amplifier. From Equation (6), it is obvious that  $R_5, R_6, R_7,$

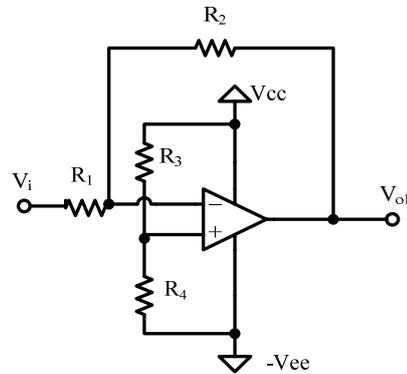


Fig. 4 The inverting amplifier

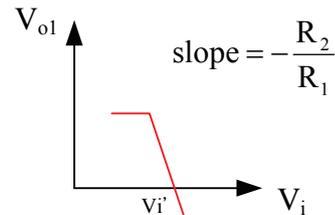


Fig. 5 The transfer curve of the circuit in Fig.4

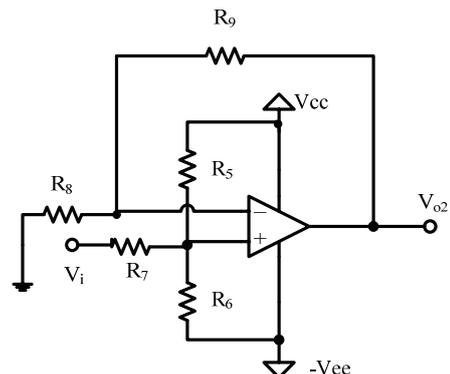


Fig. 6 The noninverting amplifier

$R_8$ , and  $R_9$ , control the slope. While from Equation (7), the horizontal intercept is controlled by resistors  $R_5$ ,  $R_6$ , and  $R_7$  and  $V_{cc}$ .

3. The operational amplifier-based fuzzy membership function

A fuzzy membership function circuit employing OPAs is proposed in Fig. 8. The circuit consists of an inverting amplifier, a noninverting amplifier and a superdiode. The greatest advantage of the circuit which constructed the membership function is with few components and two power supplies. The circuit has the advantages of low cost and high efficiency. In Fig. 8, the noninverting amplifier and the inverting amplifier have the same input  $V_i$ .

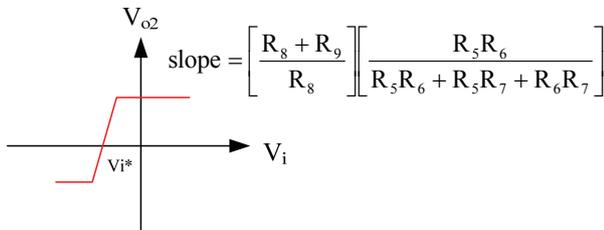


Fig. 7 The transfer curve of the circuit in Fig. 6

The output of the above mentioned two amplifiers are combined to be the input of the superdiode. In Fig. 8, if  $R_9 = R_{10} = R$ , then the combination of the transfer curve form a function  $V_o(V_i)$  with the input  $V_i$  by using superposition theorem

$$V_o^*(V_i) = \frac{1}{2}(V_{o1}(V_i) + V_{o2}(V_i))$$

$$V_o(V_i) = \begin{cases} V_o^*(V_i) & \text{if } V_o^*(V_i) \geq 0 \\ 0 & \text{if } V_o^*(V_i) \leq 0 \end{cases} \quad (8)$$

where  $0 \leq V_o(V_i) \leq V_{o,max}$ .  $V_{o,max}$  is the maximal value of  $V_o(V_i)$ . The membership function  $F(V_i)$  can be defined by  $F(V_i) = [V_o(V_i)] / V_{o,max}$  with  $0 \leq F(V_i) \leq 1$ .

V. SIMULATION RESULT

HSPICE is used to simulate the circuit shown in Fig. 8. The simulation result is shown in Fig. 9. From the proceeding narration, the slope of the different parts of the membership function curve can be controlled independently and are equal to halves of the single OPA output ends. The whole output curve crosses over the positive region and the negative region. The two kinds of characteristics keep this circuit more flexible for industrious applications.

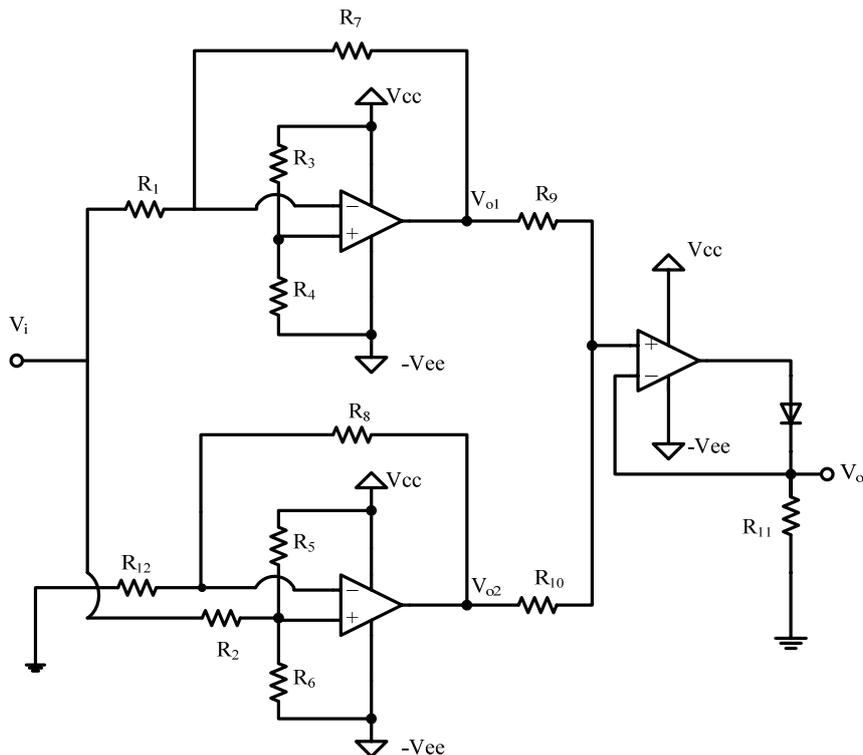


Fig. 8 The operational amplifier-based fuzzy membership function

## V. CONCLUSION

The proposed circuit achieves fuzzy membership functions with few components of OPAs, superdiode and power supplies in discrete circuit compared with [9]. And so the cost reduced. Fuzzy membership function can be controlled easily by variable resistors and power supplies. Because OPAs are very popular in industry and Fuzzy membership function is very important in many fields as [10-14], the proposed circuit is very important to construct a fuzzy analog circuit.

## ACKNOWLEDGEMENTS

We appreciate the assistance of CHUN-MING CHANG, CHEN-CHUAN HUANG and YUNG-CHANG YIN. They give us many suggestions and make some simulations for the research.

## REFERENCES

- [1] L. A. Zadeh, "Fuzzy algorithms," *Information and Control*, vol. 12, pp. 94-102, 1968.
- [2] T. Yamakawa, "A programmable fuzzier integrated circuits-synthesis, design, and fabrication," *Information Sciences*, vol. 45, pp. 75-112, 1988.
- [3] S. -I. Liu, D. -S. Wu, and H. -W. Tsao, "Nonlinear circuit application with current conveyors," *IEEE Proceedings-G*, vol. 140, no. 1, Feb. 1993.
- [4] D. V. Lindley, "Scoring rules and the in-avoidability of probability," *International Statistical Review*, vol. 50, pp. 1-26, 1982.
- [5] M. Tribus, Comments on "fuzzy sets, fuzzy algebra and fuzzy statistics," *Proceedings of the IEEE*, vol. 67, no. 8, pp. 1168-1169, 1979.
- [6] S. -I. Liu, Y. -S. Hwang, and J. -H. Tsay, "CCH based fuzzy membership function and max/min circuit," *Electronics Letters*, vol. 29, no. 1, 7 Jan. 1993.
- [7] A. Kandel and W. Byatt, "Fuzzy sets, fuzzy algebra, and fuzzy statistics," *Proceedings of the IEEE*, vol. 66, no. 12, pp. 1619-1639, 1978.
- [8] B. Kosko, "Fuzziness vs. probability," *Int. J. of General Systems*, vol. 17, no. 2, pp. 211-240, 1990.
- [9] T. Inoue, T. Motomura, R. Matsuo, and F. Ueno, "New OTA-BASED analog circuit for fuzzy membership functions and max/min operations," *IEICE Trans.*, vol. 74, no. 11, pp. 3619-3621, 1991.
- [10] L. A. Zadeh, "Fuzzy sets as a basis for a theory of possibility," *Fuzzy Sets and Systems*, vol. 1, pp. 3-28, 1978.
- [11] L. A. Zadeh, "Outline of a new approach to the analysis of complex systems and decision process," *IEEE Trans. Syst. Man Cybern.*, vol. 3, no. 1, pp. 28-44, 1973.
- [12] H. -J. Zimmermann, *Fuzzy Set Theory and Its Applications*, Kluwer Academic, Dordrecht, 1991.
- [13] D. Dubois and H. Prade, *Possibility Theory*, Plenum Press, New York, 1988.
- [14] M. S. Yang, "On a class of fuzzy classification maximum likelihood procedures," *Fuzzy Sets and Systems*, vol. 57, pp. 365-375, 1993.

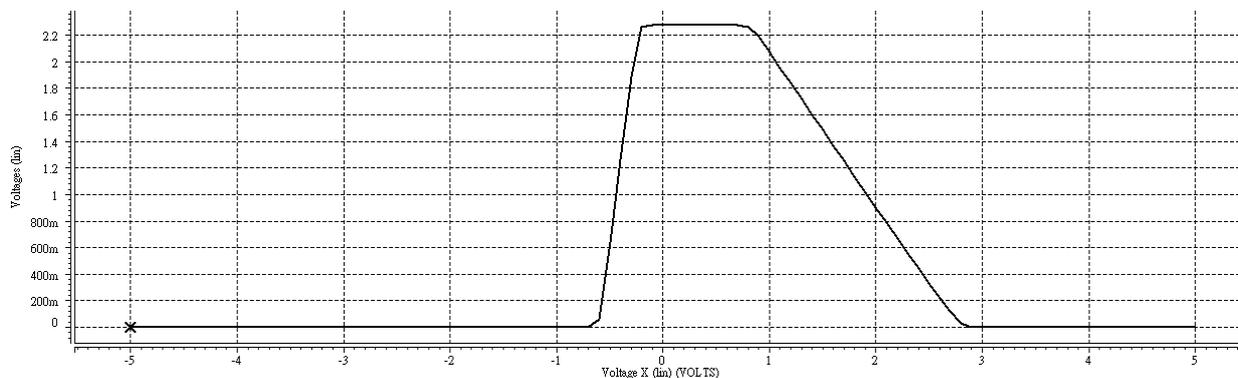


Fig. 9 The simulation result